On Several Social Network Analysis Problems: a Report

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Abstract In this paper we describe our approach to several problems offered at the ACM SIGMOD Programming Contest 2014. These problems belong to the area of a social network analysis and involve several types of queries to a social graph. The considered graph is modeled by the standard SNB benchmark. We briefly introduce this benchmark, the contest and the problems. Next, we describe our contribution, which is the following: the algorithms for evaluation of these queries and their efficient implementation. Furthermore, we present parallelization techniques for these algorithms and describe overall architecture of our solution.

1 Introduction and Related Work

In this paper we study several problems offered at the ACM SIGMOD Programming Contest 2014 [1], a yearly programming contest focused on a data management topics.

This contest has a number of features, which distinguish it from a well-known ICPC series:

- Participants are offered some science-intensive task, which is usually an unsolved problem of current importance.
- The contest runs for several months and no on-site participation is required.
- Topic specificity — the clear data management focus is present. For example, contests of previous years involved construction of distributed query processing engine (2010), multidimensional index (2012) or document stream filtering system (2013).
- The participation is allowed to both graduate and undergraduate students, without any restriction on a number of attempts.

While this contest is not so well known as the ICPC, it is nevertheless popular. For example, last year there were more than 100 registered teams. The contest is relatively young — it runs for 6^{th} time this year.

In this paper we also describe the contest: the rules, the task, its timeline and required qualifications. Moreover, we present our experiences and provide a solution of the team "GenericPeople" (Ilya Shkuratov and Vsevolod Sevostyanov), which was ranked[1] 17 out of 33 teams on the preliminary (public) tests. While our approach is not the best, it still has merit:

[1] http://www.cs.albany.edu/~sigmod14contest/leaders.html, last accessed 02/05/2014.

– our solution can serve as an example demonstrating the required qualifications and which may help to assess the required effort and work intensity. These factors may be of interest for a person who is thinking about the participation;
– the solution successfully passed through all available tests (datasets of three different sizes) within the time limits specified by the contest organizers (5 and 10 minutes);
– the proposed algorithms passed all correctness tests;
– parallelization techniques of these algorithms may be of interest;
– the number reported in the leaderboard is the sum over all query types, at the present time we can say nothing regarding their individual performance;
– at last, the number was reported for three datasets; the proposed algorithms may behave differently (better or worse) on another dataset.

Thus, we deem current study as worthy to be presented and of some interest for the reader. Another motivation for this paper is the concise presentation of the solution for the contest problem, which is usually lacking. After the contest all what is left are the posters of the top five performing teams without detailed explanation (it is given orally at the conference). Also, these posters are (or at least were in the past years) not going into the conference proceedings and are kept on a website, which may disappear. Moreover, we present our experiences and describe (at least partially) the way we went through in order to produce a working solution. It is impossible to pass on all these aspects via poster.

This year contest was dedicated to a social network analysis topic. Social network is essentially a graph, whose vertices represent users and edges denote relations between them. An example of such relation may be "know each other", "follow" and so on. Additionally extra information like a place of work or study, geographical information, various tags, images, likes etc. is known.

In the past years massive amounts of such information were made available for analysis, forming a strong incentive for both academy and industry to come with means for its efficient storage and processing. Social data play a significant role in the whole "Big Data" movement.

A lot of analysis tools employ the MapReduce [6] programming model. Industrial examples of such systems are PIG (Yahoo) [13], SCOPE (Microsoft) [5], Hive (Facebook) [18], Dremel (Google) [14]. Academic examples are Starfish [9], HadoopDB [3] and many others[2]. An alternative (which can be considered a poor man's solution) sometimes employed in production environment, is to use scripts written in scripting language like Python to commence the analysis. A data scientist has to analyze the problem and implement all necessary algorithms manually. While it may not favor the rapid development, it may allow to achieve a more efficient processing. Naturally, this approach is more flexible than using a standard tool and allows a fine-tuning of algorithms. However, it requires extensive technical expertise: knowledge of algorithms and data structures, the understanding of the data processing and so on. The tasks of the contest are representative examples of this "manual" approach and can be considered as a training for a data scientist.

[2] A list can be found in `http://dl.acm.org/citation.cfm?id=1454166`, last accessed 22/07/2014.

Another aspect of the contest task is the graph analysis component. Graph analysis is a mature area of research which studies the efficient storage and processing of graph data. There are several graph database management systems (a special type of DBMS) and graph programming frameworks. These DBMS feature special query languages, query processing algorithms and data storage.

Some examples of the graph DBMS are Neo4j [12], InfiniteGraph [10] and the framework examples are Apache Giraph [2], Signal/Collect [17]. It is necessary to mention that two latter systems also follow the MapReduce model.

The contestants were given the task which consists of the datasets and four types of queries. The social graph was generated using the SNB [16] tool.

The goal was to develop a program which computes the results as fast as possible. The contestants had not only to devise the algorithms for efficient query processing on a large graph, but also to parallelize them. This is a must, given the fact that the evaluation of the resulting implementation was performed on a server-class equipment (8 cores).

Another important aspect was the order of computation for each sub-query. The contestants had to bear in mind the size of intermediate results and the memory bound. In other words, the contestants had to perform the work of a query optimizer: gather needed statistics, assess selectivities and develop an optimal processing strategy for each query type. Also, given the hardware multi-core capability, efficient inter-query type orders are also of interest.

The contribution of this paper is the following:

- The description of the ACM SIGMOD Programming Contest 2014 and its task;
- The contest from the participant's point of view: our experiences;
- The algorithms to handle the problems offered at the contest;
- A parallelization techniques for each of these algorithms;
- A general system architecture: subquery computation orders, inter-query type orders and chunk-based data loading.

Now, we are going to describe our experiences. The task description, SNB description and its data schema, the data statistics are presented the appendix section.

2 Contest description and experiences

Let's describe this year contest from the participants' point of view. We have already briefly described the contest and its specifics in the introduction section. You can find detailed information regarding the ACM SIGMOD Programming Contest series in the reference [19].

Our research group is a frequent participant of this contest; we had achieved good results twice in the past: in the 2010[3] (team "spbu") and 2013[4] (team "Rota Fortunae") year. Both times our teams achieved 3^{rd} place in the final ranking.

[3] `http://dbweb.enst.fr/events/sigmod10contest/results/#winner`, last accessed 22/07/2014.

[4] `http://sigmod.kaust.edu.sa/finalists.html`, last accessed 22/07/2014.

2.1 General information

This year contest followed the general scheme described in the reference [19]. However, there were several notable divergences:

1. The contest started noticeable later compared to previous years;
2. There were no 2^{nd} round, unlike early years. This change happened in 2013;
3. The absence of the dedicated correctness testing phase during the evaluation (it was performed concurrently with the performance evaluation);
4. There was a series of datasets which were progressively disclosed by the organizers, as the performance of the submissions improved;
5. The task did not explicitly required parallelization or concurrency support, but instead, implied it. It was possible to submit purely sequential implementation;
6. It was possible to submit only the executable, without source code during the preliminary evaluation. The final evaluation required source code and this led to some compatibility difficulties;
7. Contestants were allowed to choose programming languages other than C++.

The provided task was a science-oriented problem related to social network analysis. The problem was to execute a number of queries to a graph representing some social network. The goal was to produce a correct answer and minimize the overall processing time. The graph and queries are fully described in the next section.

Below you can see the timeline of the contest.

– January 25, 2014 — Contest announced.
– February 1, 2014 — Detailed specification of the requirements and test data available.
– February 16, 2014 — A medium data set (10k people) with query workload and answers are available on the Task page. New query workload and answers for the small data set (1k people) are available on the Task page.
– March 1, 2014 — Team registration begins. Leaderboard available.
– March 11, 2014 — Workloads on a medium data set (10k people) have been added to the evaluation system.
– March 17, 2014 — Workloads on a large data set (100k people) have been added to the evaluation system.
– April 15, 2014 — Final submission deadline.
– May 15, 2014 — Finalists announcement.
– June 22-27, 2014 — Conference: announcement of the winner and the poster presentations.

In the overall the contest run for two and a half months. Also you can see that several datasets were progressively added to the evaluation pool. These datasets were progressively disclosed by the organizers as the performance of submissions improved. This is a rather new model of evaluation (appeared in 2013 contest) and it was employed in the following way. As soon as the several submissions were achieving some performance level, where it was hard to discern their quality due to inaccurate measurements (thread scheduling effects, for example), a new, larger dataset was added.

2.2 Communication with the contest organizers

Information about the order and rules of the contest were provided on a special web page [1], which was the main mean of communication between the organizers and the contestants. It also describes test data sets, the task and an evaluation environment. Later opportunities to register a team and submit solutions were added.

The organizers also created a Google Group in order to discuss any technical issues (e.g. code page problems) and to provide additional information that might be of interest to all of the contestants: test data-sets publication dates, disk space availability, size of data set for the final evaluation and so on.

2.3 Required skills and our experiences

Since the organizers of the contest considers Linux as its target platform, we decided to use C++ programming language as it looks to us an highly-optimizable one. Those who want to take part in the contest are advised to learn Linux development utilities such as gcc, make, valgrind (especially callgrind might be useful), gdb, etc. Also two bash scripts were required: one should build the solution and the other — run it with certain parameters.

You also may encounter restriction on size of submitted solution. It was 8 MB this year, thereby it was helpful for us to learn a couple of gcc flags. The first one is *-s*. It removes unneeded symbols from an executable, thus reducing its size without the loss of performance. The second flag may be useful, if you use external libraries: *-MM* instructs the compiler to generate source files dependencies. This helped us to familiarize with boost headers dependencies, strip boost from unneeded header files and further reduce submitted archive size.

Understanding compiler optimization methods may be of use as well. It allowed us to cope with the gcc optimizer bug, namely incorrect copy propagation after global common subexpression elimination pass. It leads to usage of the original pointer to the buffer instead of its copy, which cause segmentation fault on an attempt to free this buffer. The workaround is to add a dummy use of the original pointer after working with the buffer.

Another important skill is an ability to find necessary information on the subjects of the competition, i.e. the ability to work with digital libraries. Usually the task of the competition (or one of the tasks) is an unsolved scientific problem. Thus one may find useful information about methods have been tried or perspective approaches. These gave us several hints for the given task.

2.4 Tools

Aside from the usual requirements this year contest posed an additional one: knowledge of some scripting language or a tool for data analysis. This language can be used for datamining: to detect hidden dependencies in the source data and collect necessary statistics. We used python programming language, other examples include R and Octave tools.

2.5 Data

The schema for the data used in the task formulation is presented on Figure 1. Data were stored as a set of CSV files. It is worthy to mention that not all of the files were needed for the query processing. Also, organizers had provided data only for two datasets — the one containing thousand and the one containing ten thousand of persons. These datasets are sufficient for the debug purposes, but they are not enough to tune algorithms for the final evaluation, which involved a graph of million of persons. The benchmark generation parameters were kept in secret and it was impossible to generate that graph by ourselves.

3 Algorithms

In the rest of this paper we refer to the graph induced by "know each other" relation as $graph$, and to the breadth-first search of that graph as BFS. This graph is used in every query type and BFS (as we show further) plays the key role in all of them. Thus, a shorthand notation would be useful. The rest of notation can be found in Table 1.

3.1 Query Type 1 (Shortest Distance Over Frequent Communication Paths)

Algorithm description An obvious strategy for evaluation of such query would be the following:

1. Run BFS from person $p1$ to person $p2$ and return hops count;
2. During the BFS traversal one needs to check the replies condition. For each edge, considered on a given BFS step, one has to calculate the number of mutual replies for the corresponding persons. If it is less than k, then the transition is not possible — the edge does not exist.

This "naive" approach needs no preparation and can be ran just after the $graph$ construction. For each pair of adjacent persons it is necessary to calculate the number of replies and this may take some time. Thus, the described BFS has the complexity $O(m \cdot n \cdot (|V| + |E|))$ where n denotes a cardinality of "comment is reply of comment" relation and m — cardinality of "comment has creator person".

Therefore, we propose a pretreatment phase that will compute number of replies once, which effectively eliminates the repeated calculations. Our goal is to find persons that made *not less than* k comments replying to each other. For each pair of persons connected by an edge e in the $graph$ we will determine the number of mutual replies k_e and attribute it to e. In this way, BFS on each step compares two numbers: given k and pre-calculated k_e.

Algorithm details Data preparation. We transform relation "comment is reply of comment" into "person replied to person" using "comment has creator person" and then count number of replies for each element in the resulting relation.

First, file "comment has creator person" is parsed and represented as map $ccreat : comment \mapsto creator$ in order to reduce comment owner search time. Second, since the file representing "comment is reply of comment" is one of the largest generated by

the SNB it is of use to distribute its processing between separate threads. Each thread calculates a local result λ and then all local results are merged into replies map

$$\Lambda : (person1,\ person2) \mapsto \\ \mapsto (\text{replies of } person1 \text{ to } person2, \\ \text{replies of } person2 \text{ to } person1).$$

Next, from the replies pair minimal coordinate is chosen (we previously denoted that value k_e) and ascribed to the edge between $person1$ and $person2$. For those persons who hasn't written any replies to each other, k_e is set to 0. The proposed data preparation procedure has the complexity $O(m + n + |E|)$.

BFS. Now we have sufficient information to tell whether a pair of persons has at least k mutual replies. With this information at hand, BFS makes only one numeric comparison per hop. Therefore, BFS complexity is reduced to $O(|V| + |E|)$.

Algorithm 1: LOCAL REPLIES PROCESSING

```
1  function q1_local(crepl, ccreat)
       input: crepl — part of file comment is reply of comment,
              ccreat — map comment ↦ creator
       output: λ — local result, same type as Λ
2      reply_ID ⟵ read_next(crepl);
3      comm_ID ⟵ read_next(crep);
4      while not eof(crepl) do
5          r_owner ⟵ ccreat[reply_ID];
6          c_owner ⟵ ccreat[comm_ID];
7          first ⟵ min(r_owner, c_owner);
8          second ⟵ other;
9          if ∃(first, second) in λ then
10             increment coordinate in λ[first, second] according to reply direction;
11         else
12             λ ⟵ (first, second) ↦ (1, 0) or (0, 1) according to reply direction;
13     return lambda;
```

3.2 Query Type 2 (Interests with Large Communities)

In order to efficiently evaluate this query type one has to efficiently perform the search for connected components on a $graph$.

A general idea This query type is evaluated using the graph which is derived from the $graph$ by applying two additional restrictions. The first one states that all vertices should share a common tag and the second one requires the birthdate of every vertex (person) to be later or equal than a date d. In this filtered graph we should search for connected components. The straighforward approach is to check these restrictions during the graph traversal. This means we should traverse the whole graph for each tag. The complexity

Algorithm 2: GLOBAL REPLIES PROCESSING

```
1  function q1_global(graph, crepl, ccreat, threads_number)
       input: graph,
              crepl — file comment is reply of comment,
              ccreat — map comment ↦ creator,
              threads_number
2      array p ⟵ split crepl into threads_number parts;
3      for j ⟵ 0 to threads_number do
4          create_thread(q1_local(p[j], ccreat));
5      for j ⟵ 0 to threads_number do
6          merge(Λ, join_thread(j));
7      for e in graph do
8          p1 ⟵ e.start();
9          p2 ⟵ e.end();
10         k_e ⟵ min(Λ[(p1, p2)].f, Λ[(p1, p2)].s);
```

of this approach is $O((|V|+|E|)\cdot|T|)$. Now, lets consider other approaches to restriction checking.

The common tag requirement. In order to handle this restriction an index *tag-person* using the person_hasInterest_tag relation can be built. One should not worry about hitting the memory bound. Table 3 shows that the number of tags is increasing slowly, on average a person has 3.5 interest tags in graph containing 1000 persons, as well as in graph containing 10000 persons. Thus, we assume this ration will stay the same during the further graph size increase. Using these numbers we can estimate the size of the index for a graph containing million persons: $((4500 \cdot 9) + (1000000 \cdot 3.5)) \cdot (8/1024/1024) \approx 27$MB.

This index is represented by a hash-table (implemented by boost::unordered_map collection). It allows to efficiently construct and query the index, having constant insert and access complexity [4].

Birthdate. We can reduce the number of constraint checks by pre-filtering persons (vertices) who were born earlier than a given date. These excessive checks happen during the processing of arcs which lead to the aforementioned vertices. Thus, it may be impractical to construct the whole new graph. Indeed, suppose we are given a person which has ten friends which share the common tag. In this case when we will check this vertex eleven times (adding one more time for index look-up during BFS initiation). But if we properly exclude it from the neighboors of these ten nodes, we would have to check it only once.

Thus, in order to accomplish the pre-filtering, we would exclude not the vertices but the edges incident to them. We call this process "date pre-filtering" and the resulting graph — "graph time slice", or simply "time slice". This approach allows us to keep arrays of such edges in our graph. The resulting increase of the memory requirements is tolerable; this form of storage would require not more than two times the space of the original graph. It is acceptable even for a graph with a million vertices.

However, this approach requires a preprocessing phase because every query would require its own time slice, which would lead to additional costs synchronization (in case of multithreaded approach). If we would manage to avoid preprocessing phase, we would be able to run several queries consequently and without synchronization. This will lead to a better load balancing because the thread, which had finished its part of work for a previous query, can immediately start processing next query without waiting for others. We will refer to this type of processing as "continuous processing".

It is impossible to create all of the time slices to avoid preprocessing due to memory bound. But it is possible to create several of them and later use the one which contains d. If the time slices form the decomposition of the whole graph time range (complete, pairwise disjoint) G_t and the graph contains million persons, this approach would additionally require $22.8 \cdot (N-1)$ MBs (compared to a single time slice), where N is the number of time slices. Thus, we managed to avoid preprocessing phase using rather small amount of memory and sacrificing some accuracy of the time slice.

Query processing Index construction. The index is constructed using the file *person_hasInterest_tag*, which defines the corresponding relation. This file is being parsed and pairs *(tag_id, person_id)* are being inserted into hash-table, with the key being *tag_id*, and the value — array of *person_id*.

The index is being constructed using one thread because the file *person_hasInterest_tag* is rather small and there would be a considerable overhead which is not covered by the gain (for a large datasets it is possible that parallelization will pay off).

Time slice construction. We had studied the distribution of the persons over time (see Table 2) and suggested that there is a uniform distribution. Also, the contest organizers stated nothing regarding the query parameters. Thus, we considered d as a uniformly distributed random variable. On that basis we decided to produce time slices of equal length.

There are two stages of time slices construction:

- On the first stage we determine the time slice which should contain a given person. In all of the datasets the whole time range was eleven years (1980 – 1990 years). In order to keep the balance between time slice accuracy and memory expenses, we decided to split the whole range in six slices: five of them span two years and the last slice — one year.
- On the second stage the time slices are constructed (see Listing 3). It is easily parallelizable because all of the modifications which are performed in the graph vertices are independent of each other.

Community cardinality computation Let's first describe the sequential algorithm and then discuss its parallelization.

Sequential algorithm. Before we start to loop over tags, we initialize a structure for the result by specifying the maximum number of tags it should keep (line 2), then we scan all tags (lines 3 – 9). For each tag we get the cardinality of the largest connected component using the BFS (lines 4–8) and put it into the resulting list (line 9).

Algorithm 3: TIME SLICE CONSTRUCTION

```
1 function slice(graph)
      input: social network graph graph
2     foreach person in graph do
3         foreach friend of person do
              /* insert friend to person's slices array that corresponds
                 to friend's slice id                                    */
4             person.slices[friend.slice_id].add(friend)
```

Algorithm 4: FIND TOP-K INTEREST WITH LARGE COMMUNUTIES. SEQUENTIAL.

```
1  function query2_linear(tp_index, query)
       input: tag — person index tp_index, query parameters query
       output: top-k list
2      top_k_tags.init(query.k);
3      foreach (tag, person) in tp_index do
4          component_size ⟵ 0;
5          foreach person in Persons do
6              if person is visited then
7                  new_size ⟵ BFS(person, query.date);
8                  component_size ⟵ max(component_size, new_size);
9          top_k_tags.insert(component_size, tag);
10     return top_k_tags.get_top_k_tags();
```

Parallel algorithm. We tried to minimize the overheads of synchronization when we were parallelizing the algorithms. In order to achieve this one has to minimize the amount of shared resources. In our case this shared resource is the *top_k_list*, which we decided to keep as a thread-local *top_k_list*. Threads construct a partial results independently and then one merges them in order to get the final result. Since we managed to avoid the preprocessing phase, the queries can be processed in blocks, e.g. without barrier synchronization between two consequent queries. Also, it is possible to delay the evaluation of the final result until the end of the query block. Basing on the amount of memory, which we are ready to dedicate for partial results, we can determine the size of the block. We assumed that the number queries of the second type would be low, so we grouped all of them in one block. We can name two advantages of this approach:

- no synchronization is needed in order to form the final result for each query;
- it is possible to parallelize the construction of the final results.

Thus, we eliminated excessive synchronization and increase the number of operations which can be executed in parallel.

Listing 5 and Listing 6 describe the parallel approach. Algorithm described in Listing 5 differs from the sequential counterpart in the tag distribution between threads (for this purpose a thread id and the total number of threads are used). Here, we assume that the threads id range from 0 to $N - 1$, where N is the total number of threads. In the algorithm Listing 6 we describe the getting of the partial results (line 3) and their merging (lines 5 – 8).

Algorithm 5: FIND TOP-K INTEREST WITH LARGE COMMUNUTIES. PARALLEL.

```
1  function query2_parallel(query, tp_index, th_info)
       input: query parameters query,
              tag — person index tp_index,
              thread information th_info,
              (th_info.id — thread id,
              th_info.count — total number of threads)
       output: partial result for query partial_result
2      int position ⟵ th_info.id;
3      partial_result.init(query.k);
4      while position < tp_index.size do
           /* Get pair (key, value) from index at position                    */
5          (tag, persons) ⟵ tp_index.get(position);
6          foreach person in persons do
7              if person is visited then
8                  new_size ⟵ BFS(person, query.date);
9                  component_size ⟵ max(component_size, new_size);
10         partial_result.insert(component_size, tag);
11         position ⟵ position + th_info.count
12     return partial_result;
```

Algorithm 6: QUERY TYPE 2 EXECUTION

```
1  function evaluate_query2(QL2, tp_index, th_info)
       input: list of queries type 2 QL2,
              tag — person index tp_index,
              thread information th_info,
              (th_info.id — thread id,
              th_info.count — total number of threads)
       output: results for block of queries type 2 q2_results
       /* Queries evaluation                                                  */
2      foreach query in QL2 do
3          q2_part_results[query.num][thread.id] ⟵ query2_parallel(query,
           tp_index, th_info);
4      barrier;
       /* Merging the partial results                                         */
5      int position ⟵ th_info.id;
6      while position < QL2.size do
7          q2_results[position] ⟵ merge(q2_part_results[query.num]);
8          position ⟵ position + th_info.count
9      return q2_results;
```

Possible improvements Further improvement may be achieved through tag sorting by a number of persons with this tag (storing the lower bound). While looping we can check whether there are enough persons with the given tag left in order for the result to enter the *top-k*.

3.3 Query Type 3 (Socialization Suggestion)

Algorithm description. The common sense may provide the following idea of the straightforward evaluation:

1. for each vertex v in the $graph$ perform BFS while keeping in mind the given hops count h;
2. upon completion BFS returns the list of reached people rp;
3. for v and each person v_r from rp check information about their work places, study places and location for correlation with p;
4. if one of the places where both v and v_r are involved is p or its subplace, then calculate the number of common interests ci;
5. store (sorted by ci) the resulting pairs (v, v_r);
6. return the top-k pairs as a result.

This algorithm requires examination of all the persons returned by BFS. Since $graph$ is a social its edge count follows power law, therefore there are some hubs and connectors with large degree and many vertices with only a few incident edges [11]. Hubs and connectors shorten the paths between persons and thus, the size of rp may be significant. The time complexity of this algorithm is

$$O(|V| \cdot (|V| + |E| + |rp| \cdot |person.places| + |person.interests|)).$$

It is desirable to reduce the number of persons to examine without the loss of result correctness. In order to do that we suggest to group persons by some of place types. SNB provides three place types: $city$, $country$ and $continent$. There are only five continents and such a fragmentation won't be useful in context of fast-growing $|V|$. On the contrary, grouping by $city$ leads to lots of small groups that take large amount of space. Thus, $country$ seems to be a good choice which causes medium number of satisfactory-sized groups (about 111 countries for 1k vertices). Furthermore, study places and location of person are represented by $cities$ and work places — by $country$, respectively. Thus, we can easily make all three place classes identical using "place is part of place" relation, provided by SNB.

But still if the type of p is $continent$, we will have to iterate the whole $graph$. There are several solutions to this problem, some of them are the following:

1. for each continent store all countries that are situated on it;
2. for each person store continents which are associated with that person.

The first solution is not as space consuming as the second yet requires more time. For each person it is necessary to run BFS several times (one for each $country$) or for each hop to check whether any of the person's places belongs to a given $continent$.

The second solution has a great advantage: for each BFS hop it takes only a few numeric comparisons to check the required condition. Every person will require at max 5 integers of additional storage, so such approach is affordable and will not dramatically increase $graph$ representation's size. Let's denote BFS that returns reached persons from the given $country$ as gBFS and BFS that returns reached persons from the given $continent$ as cBFS.

Using the proposed partitioning we suggest a following algorithm:

1. use the type of p determine which group g (continent $cont$) to process;
2. for each person v from this group (continent) perform gBFS (cBFS) bearing in mind the given hops count h;
3. on completion gBFS (cBFS) returns the list of reached people rp;
4. for v and each v_r from rp calculate the number of common interests ci;
5. store (sorted by ci) resulting pairs (v, v_r);
6. return the top-k pairs as a result.

Described approach time complexity is

$$O(|persons\ in\ p| \cdot (|V| + |E| + |rp| \cdot |person.interests|)).$$

Algoritm details. Relation "place is part of place" will be frequently accessed so it seems beneficial to implement it as a map $sm : place \mapsto parent$. Each vertex contains two sets of places: (i) study places and location, (ii) work places. We follow such partitioning scheme with regard to the place types mentioned above. Each person has a set of $continents$ that are simply deduced from this person's places using sm. Groups by $country$ place type are created during $person \times place$ relations parsing. We implement set of groups as a map $\Gamma : place \mapsto$ set of $persons$. Though elements of Γ may intersect, it is convinient to iterate trough and sets keep only unique persons in each group. Preparations have complexity $O(n+m)$ where n stands for cardinality of "place is part of place" and m for summary cardinality of $person \times place$ relations.

The full processing scheme for query type 3 is presented in the following algorithms: 9, 10, 11 and 7. Due to the space constraints the first three of them are presented in the appendix.

3.4 Query Type 4 (Most Central People)

Index construction In order to ensure the fast construction of the graph needed for *closeness centrality* computation we decided to build index *tag - person*, which maps each tag into a set of persons who are members of the forum having such tag. We set up this index using the standard C++ containers *C++ map* and *set*, which are implemented using the red-black tree. These containers were chosen due to the two reasons. First, this index should reside in the main memory. Second, in order to efficiently construct graph for a given tag we need sorted sequence of person ids. If we use a tree-based index, the sorting happens during the index construction. It is worthy to mention that index was built only for tags which were needed for the query execution: there were only a few queries of this type in the workloads, but the number of forums were rapidly increasing.

Algorithm 7: Query3 evaluation

```
1  function query3(graph, h, k, p)
       /* top-k is a set with some priority that orders pairs by ci, it
          only keeps not more than k elements at every moment          */
2      ptype ⟵ type of p;
3      if ptype is continent then
4          for v in graph do
5              if not v in p then
6                  continue;
7              rp ⟵ cBFS(v, p);
8              for v_r in rp do
9                  ci ⟵ get_ci(v, v_r);
10                 pair ⟵ (v, v_r) in lexicog. order;
11                 top-k ⟵ (pair, ci);
12     else
13         g ⟵ Γ(p);
14         for v in g do
15             rp ⟵ gBFS(v, g);
16             for v_r in rp do
17                 if ptype is city and not v in p then
18                     continue;
                       /* rp contains people from the whole country, not
                          only p                                       */
19                 ci ⟵ get_ci(v, v_r);
20                 pair ⟵ (v, v_r) in lexicog. order;
21                 top-k ⟵ (pair, ci);
```

However, the relation which we are interested in — *(tag, person)* was not given explicitly, but was defined by two others: *(forum, tag)* and *(forum, person)*. Therefore, at first, we had to create two indexes of these relations: *tag - forum* and *forum - person*. These data structures aim to decrease the time it takes to *join* these two tables, to decrease the construction time of *tag - person*, and also to decrease a graph construction time for a given tag:

- An index *forum - person* was represented by a hash-table, in order to achieve look-up complexity for the *join* operation of $O(1)$.
- A *set* was used for *tag-person* index in order to get free duplicate elimination during the *join* operation and to acquire sorted sequence of person ids during the construction of a graph for a given tag.

The *join* is represented by the block "Build index" on Figure 4.

The calculation of closeness centrality metric In order to calculate the *closeness centrality* metric one needs to know the following three values for each of the graph vertices:

1. **r(p)** — number of vertices, reachable from it;
2. **s(p)** — the sum of all geodesic distances of all of reachable vertices;
3. **n** — the number of vertices in a given graph.

We should note, that our graph is an undirected graph, therefore **r(p)** can be calculated once for each connected component. Thus, the problem is how to compute **s(p)**.

An algorithm selection. Given the fact that our graphs is an undirected one and the edges are of unit weights, a simple BFS modification would suffice for the evaluation of **s(p)**. For this purpose we can label each visited vertex with the distance to the initial one. In this approach we do not increase asymptotic complexity of BFS and do not use additional memory. We would require $O(|V|+|E|)$ time and $O(|V|+|E|)$ memory. This estimation is better than estimation for many classical algorithms oriented for general cases of problem "minimal distance from one vertex to all other". For example, Dijkstra algorithm [7] for graphs with non-negative weights, based on Fibonacci heap [8] uses $O(|V|+|E|)$ memory and $O(|V| \cdot \log |V|+|E|)$ time. Moreover, our approach is easily parallelizable: we can compute **s(p)** in parallel for different vertices.

The cut-off heuristic. One can note that *closeness centrality* is inversely proportional to **s(p)** within a connected component. Indeed, it holds due to a fact that **n** is a constant for the whole graph and **r(p)** is a constant for all vertices in a connected component. Thus, we can propose a criterion for a vertex to enter the *top-k* of a given connected component which uses it's **s(p)**. Let's define a threshold:

$$\Theta = \max_{p \in current\_top\_k} s(p) .$$

Now, we can interrupt the computation of **s(p)**, if the current value had exceeded the threshold Θ.

Despite the simplicity of this cut-off heuristics it drastically decreased the evaluation time for the fourth query type. Unfortunately, we do not know the number and parameters of queries of this type during the final evaluation. But the implementation of this heuristic allowed to decrease the evaluation time for more than 380 seconds on a graph containing 100 thousand persons. The resulting time was 220 seconds.

An overall processing scheme. The algorithm presented in Listing 8 provides more detailed description for computation of *closeness centrality* for a single vertex. Its inputs are the vertex for which the *closeness centrality* should be computed, the size of the graph and the number of connected component the vertex belongs to. We perform the graph traversal starting from the vertex *source* during which we store the distances in the array *hops*. Afterwards, we use them for the computation of **s(p)** (line 14). A cut-off heuristic is implemented in the following way: the line 15 shows the checks which examine whether the given vertex can get into *top-k* and the line 17 shows the update of the threshold.

Like for query type two, the query type four is eligible for delayed computation of the final result, which allows to decrease the number of synchronizations and to increase the parallelization capability of the algorithm. But also, like in case of the second query type the the amount of memory which we can dedicate for the storage of partial results, restricts the number of queries which we can process this way. The general processing chart for a set of type four queries is presented on Figure 4. It shows the major stages and synchronization points.

Algorithm 8: COMPUTE CLOSENESS CENTRALITY FOR A SINGLE VERTEX

```
1  function BFS_q4(source, size, component)
       input: start vertex source,
              size of tag graph size,
              id of connected component which start vertex belongs to component
       output: closeness centrality of source or -1
       /* Initialization                                                    */
2      Q ⟵ source.id ;                                          // Queue
3      rp ⟵ 0 ;                                                 // r(p)
4      sp ⟵ 0 ;                                                 // s(p)
5      hops ⟵ array of -1 that size is size ;                   // distances from source
       /* BFS                                                               */
6      Enqueue(Q, source);
7      hops[source.id] ⟵ 0;
8      while Q ≠ ∅ do
9          person ← Dequeue(Q);
10         foreach friend of person do
11             if hops[friend.id] == −1 then
12                 Enqueue(Q, friend);
                   // set distance from source
                   hops[friend.id] ⟵ hops[person.id] + 1;
13                 rp ⟵ rp + 1;
14                 sp ⟵ sp + hops[friend.id];
15                 if sp > get_threshold(component) then
16                     return −1;

17     update_threshold(sp, component);
18     return rp · rp / ((size − 1) · sp);
```

The first stage was described earlier, stages 2 and 6 are trivial, stage 7 is analogous to the merge of results during the processing of the second query type. Stage 5 is the re-iteration of the algorithm presented in Listing 8 for all vertices of the constructed graph. Here, each thread processes its own set of verices. The stage 4 is the preprocessing step and is committed by one thread. On this stage the vertices are marked by the numbers their corresponding connected components, the cardinality of these components is also evaluated and initialization of data structures required for further processing is performed.

The stage number 3 constructs the graph for a given tag. The graph is represented by an array of vertices, where each vertex keeps an array of neighboor vertices. The ids of persons corresponding to each tag are distributed between threads and each thread creates a list of friends for a given person in a new graph. The only ones left are the persons who correspond to a given tag in index.

Other approaches. In the last few days of the contest we found the solution that fits almost perfectly into the described problem [15]. It is developed for directed graphs with non-negative weights and reuses the CCV of a single vertex in order to estimate CCV for other vertices and reduce the further computations. Authors also use estimates

in order to produce the cut-off of vertices which not to get into *top-k*. That method could be modified to take into account the memory restrictions. The experiments described by authors show that this approach may be particularly efficient for unweighted, undirected graph of a large size. It can reduce the amount of computations for a majority of vertices or even avoid their processing at all.

4 System architecture

Graph structure. Considering the graph structure we bear in mind the following: **(i)** the cardinality of vertices may run up to a million, **(ii)** BFS is crucial for the evaluation of every query type. Therefore, our approach must have low memory footprint and provide efficient BFS evaluation. In order to satisfy these requirements we use representation similar to adjacency lists, but with arrays instead, that is, each vertex contains a pointer to an array of adjacent vertices. It allows us to meet the memory constrains and avoid unnecessary comparisons in the BFS implementation.

Layers. Three layers may be distinguished in our implementation: **(i)** file loading, **(ii)** structure initialization and preparation, **(iii)** query evaluation.

This layered structure is rather natural to the task and allows some flexibility in the setting up the order of query evaluation. That is a rather important feature for the performance improvement. The use of the first layer is to provide the interface to chunk-based file loading. It copes with the problem of big files which can be up several gigabytes in size. The use of the second layer is to parse loaded files and to build indexes and other structures required for the query evaluation. The last layer is responsible for the final results formation.

5 Experiments

In this paper we present some experiments illustrating the performance of our approach. Unfortunately, we could not provide detailed experimental data from the contest due to several reasons: (i) we do not have access to the final benchmarks (they are not yet released to the public); (ii) we no more have access to the hardware used for the evaluation by the organizers (it was a server-class one); (iii) the two largest benchmarking query sets are unavailable too (we used the largest available dataset — the medium dataset, containing 10k persons).

Thus, we had to perform experiments on our own. The hardware and software setup was the following: i7-4930K CPU (6 cores), P9 X79WS motherboard, 4GB RAM; Ubuntu 14.04, kernel 3.13.0-24, x86_64.

The first series of experiments is presented on Figure 2. They illustrate the basic approach when we sequentially evaluate queries of the same type. The results show the contribution of each query type to the overall processing time. In this series we vary the number of threads. Eventually we get a *U-shaped* graph, which shows that it's not useful to employ more than four threads for the processing in this scenario. It is the result of the algorithm parallelization imperfection (not all algorithms use all cores all the time) and of the synchronization overheads. This leads us to the idea of pre-treatment phase

which will allow us to balance the load. The load balancing will be done by grouping tasks together into stages and reordering of query types.

To examine our idea, we had split the query evaluation into the following stages: **(i)** Q3 evaluation and Q1 preparation part 1, **(ii)** Q1 preparation part 2, Q2 preparation and Q4 preparation, **(iii)** Q1 evaluation, **(iv)** Q2 evaluation, **(v)** Q4 evaluation. Tasks belonging to one stage are executed in parallel. Figure 3 shows the results for this kind of processing. Despite that in fact we used our idea in the first two stages only, the performance boost of the evaluation with six threads is about 28% (compared to the best performance from Figure 2) and 56% comparing the performance with the six threads. This may be considered a good result for the medium dataset, which we use for testing. Efficiency of such task grouping is determined by the "closeness" of tasks executed in parallel in terms of time. The closer times of execution, the more efficiently we use the processor. We can perform the load balancing in two ways: by varying the number of threads for one task and by varying the number of tasks. Hence we can use this approach to tune performance further. However, effect of the load balancing may vary with the dataset. Taking such variation into account is rather difficult and requires a more detailed study of the data structures and the algorithms involved.

6 Conclusions

In this paper we described the ACM SIGMOD Contest 2014, its tasks, timeline and our experiences. Also we presented our approach to the offered problems and described the advantages over the naive processing. We discussed algorithms as well as parallelization techniques and presented the general system architecture. Its key points are the following: query type intermixing, query type reordering, continuous query processing and block file loading techniques.

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7 Appendix: Problems

The contest offered [1] the following problems (we fully provide them here for the better understanding of the reader and in case of the original web site outage):

1. **Query Type 1 (Shortest Distance Over Frequent Communication Paths).**
   Given two integer person ids $p1$ and $p2$, and another integer x, find the minimum number of hops between $p1$ and $p2$ in the graph induced by persons who:
   (a) have made more than x comments in reply to each others' comments (see comment_hasCreator_person and comment_replyOf_comment);

(b) know each other (see person_knows_person, which presents undirected friendships between persons; a friendship relationship between persons x and y is represented by pairs $x|y$ and $y|x$).

2. **Query Type 2 (Interests with Large Communities).**
   Given an integer k and a birthday d, find the k interest tags with the largest range, where the range of an interest tag is defined as the size of the largest connected component in the graph induced by persons who:
   (a) have that interest (see tag, person_hasInterest_tag);
   (b) were born on d or later;
   (c) know each other (see person_knows_person, which presents undirected friendships between persons; a friendship relationship between persons x and y is represented by pairs $x|y$ and $y|x$).
3. **Query Type 3 (Socialization Suggestion).** Given an integer k, an integer maximum hop count h, and a string place name p, find the top-k similar pairs of persons based on the number of common interest tags (see person_hasInterest_tag). For each of the k pairs mentioned above, the two persons must be located in p (see person_isLocatedIn_place, place, and place_isPartOf_place) or study or work at organizations in p (see person_studyAt_organization, person_workAt_organization, organisation_isLocatedIn_place, place, and place_isPartOf_place). Furthermore, these two persons must be no more than h hops away from each other in the graph induced by persons and person_knows_person.
4. **Query Type 4 (Most Central People).** Given an integer k and a string tag name t, find the k persons who have the highest closeness centrality values in the graph induced by persons who:
   (a) are members of forums that have tag name t (see tag, forum_hasTag_tag, and forum_hasMember_person);
   (b) know each other (see person_knows_person, which presents undirected friendships between persons; a friendship relationship between persons x and y is represented by pairs $x|y$ and $y|x$).

   Here, the closeness centrality of a person p is:

$$\frac{(r(p)-1)\cdot(r(p)-1)}{(n-1)\cdot s(p)},$$

   where $r(p)$ is the number of vertices reachable from p (inclusive), $s(p)$ is the sum of geodesic distances to all other reachable persons from p, and n is the number of vertices in the induced graph. When either multiplicand of the divisor is 0, the centrality is 0.

8 Appendix: SNB Description

Let's briefly survey the SNB benchmark which was used during the contest and in the experimental section of this paper.

The purpose. In order to provide efficient evaluation for a variety of algorithms, tools, frameworks for social network data management tasks, a standard benchmark, called Social Network Benchmark (SNB) [16] was developed. This benchmark allows

not only efficient, but also a repeatable evaluation for a variety of scenarios: on-line transactions, business intelligence and graph analytics. Authors of the benchmark tried to make it as realistic as possible.

Covered systems. This benchmark covers several types of systems: graph DBMS and graph programming frameworks, RDF database systems, relational and NoSQL database systems.

Data schema. The general data schema of the benchmark is presented on Figure 1 (illustration taken from [16]). It is called Social Intelligence Benchmark Data Schema. The schema uses UML notation to describe entities, attributes and their relationships of different cardinalities. The schema defines the result of the benchmark's data generator. Essentially it is a set of tables linked via primary-foreign key relationships.

The schema defines some social network and its most characteristic features:

1. users and their personal details, tags and likes;
2. relations between users (follows and knows);
3. textual content: posts and comment trees.

Generator and its output: technical details. This benchmark is essentially a synthetic data generator, which is implemented using MapReduce programming model. The generator is dictionary-based and is capable of generating correlated values. The result of the generator is the set CSV files, where each file contains records of the corresponding table.

The benchmark and the contest. The organizers of the contest used only the dataset generator, but not queries. Instead, they proposed four stand-alone types of queries, which we are describing in the corresponding section of the appendix.

The dataset generator provided four types of graph workloads: small (1k vertices), medium (10k vertices), large (100k vertices) and huge (1M vertices). The last one would be used for the final evaluation by the contest organizers.

Unfortunately, only the first two datasets were fully released to the public. The third one was discussed in the mailing list, where some of the generator parameters for this dataset were disclosed. However, no queries are known. In this paper we use the largest available (on the current date) dataset — the medium one for the experimental evaluation.

All of the queries are known at the start of the processing, contestants are not required to process them in a specific order.

9 Appendix: Experiments

Here we provide the graphs, illustrating the outcomes of our experimental evaluation. Note that Figure 2 and Figure 3 are put adjacent to each other and are situated on the same height. This allows us to examine the relative performance of these two approaches with respect to different number of threads.

10 Appendix: Miscellaneous Algorithms

This section describes miscellaneous Algorithms (Listing 9, Listing 10 and Listing 11) used for the evaluation of the query type 3.

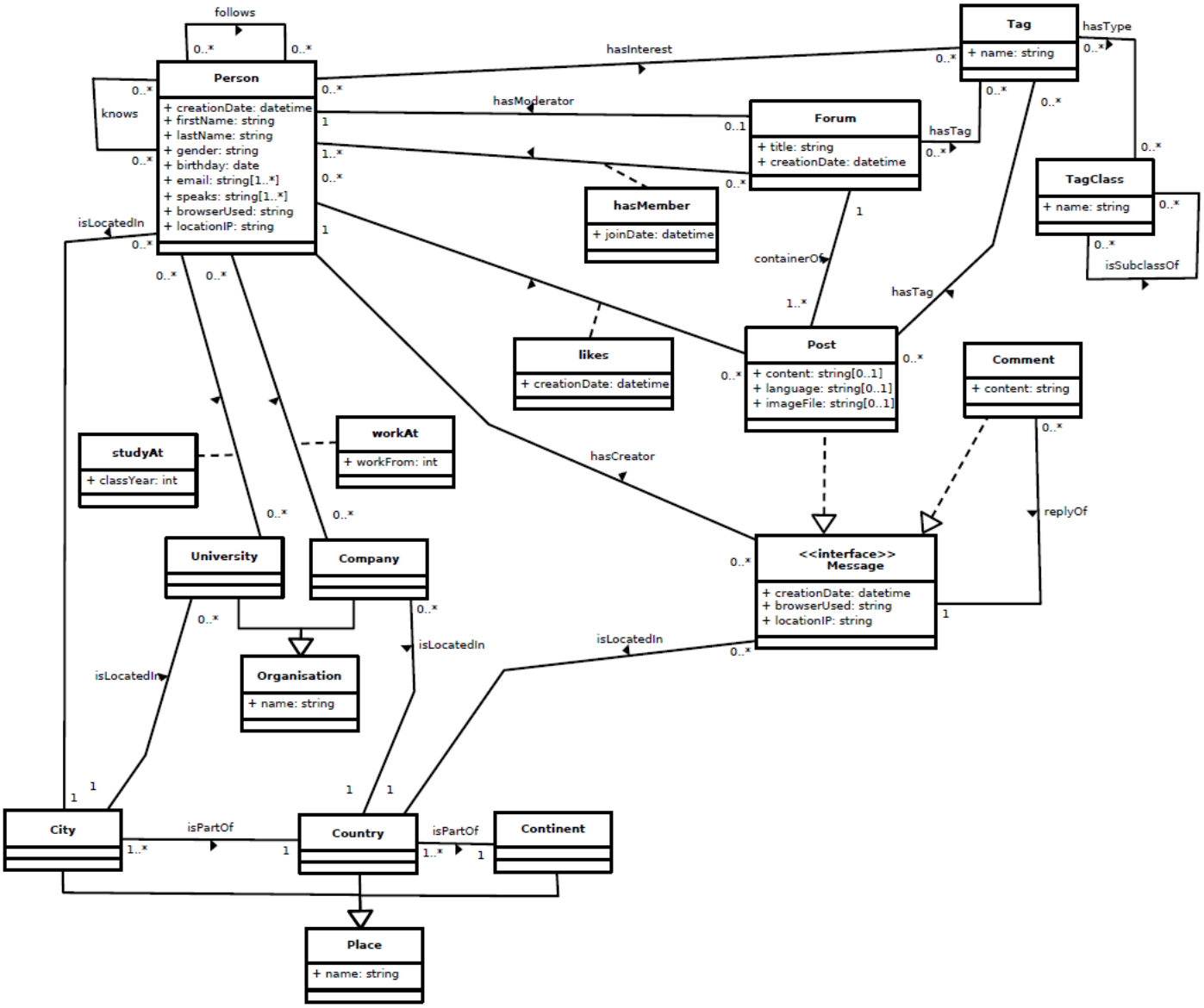

Figure 1: Social Intelligence Benchmark Data Schema

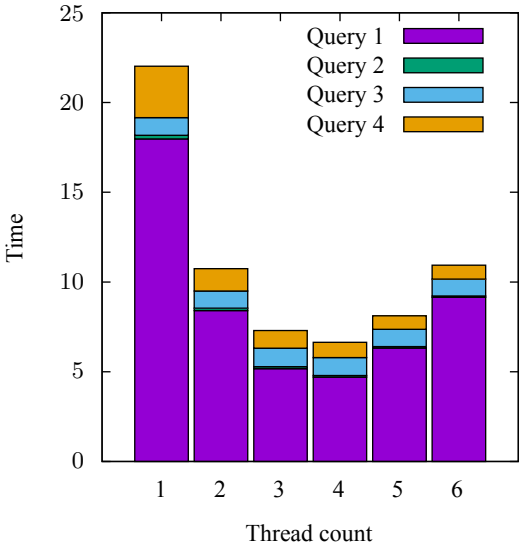

Figure 2: Performance scalability (without pre-treatment phase).

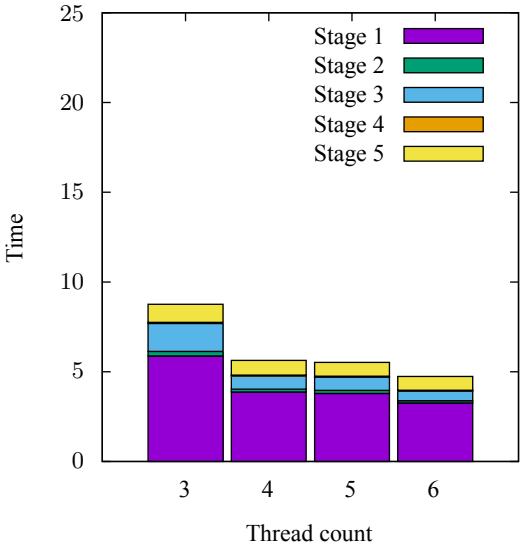

Figure 3: Performance scalability and effects of query reordering (pre-treatment phase).

Algorithm 9: LocatedIn

```
1  function located_in(places, p, sm)
       input: places — places of some person,
              p — given query parameter,
              sm — subplaces map
       output: true if places contain p or some of them is subplace of p
2      ptype ⟵ type of p;
3      setuniform ⟵ ∅;
4      if ptype == country then
5          uniform ⟵ sm[study places];
6          uniform ⟵ sm[location];
7          uniform ⟵ work places;
8      else
           // ptype is city, therefore we don't need to look in work
              places that are countries
9          uniform ⟵ study places;
10         uniform ⟵ location;
11     return p in uniform;
```

Algorithm 10: cBFS

```
1  function cBFS(source, cont, h)
       input: source — start vertex,
              cont — continent to search on,
              h — hops
       output: reached persons from cont
       /* Initialization                                              */
2      Q ⟵ source.id ;                                    // Queue
3      hops ⟵ array of -1 that size is size ;             // distances from source
4      rp ⟵ ∅ ;                                           // reached persons
5      Enqueue(Q, source);
6      hops[source.id] ⟵ 0;
7      while Q ≠ ∅ do
8          person ⟵ Dequeue(Q);
9          if hops[person.id] == h then
10             continue;
11         foreach friend of person do
12             if hops[friend.id] == −1 then
13                 Enqueue(Q, friend);
                   // set distance from source
                   hops[friend.id] ⟵ hops[person.id] + 1;
14                 if friend.continents ∋ cont then
15                     rp ⟵ friend.id;
```

11 Appendix: Query Type 4 Evaluation Scheme

In this section we present the overall processing scheme for the query type 4 (see Figure 4).

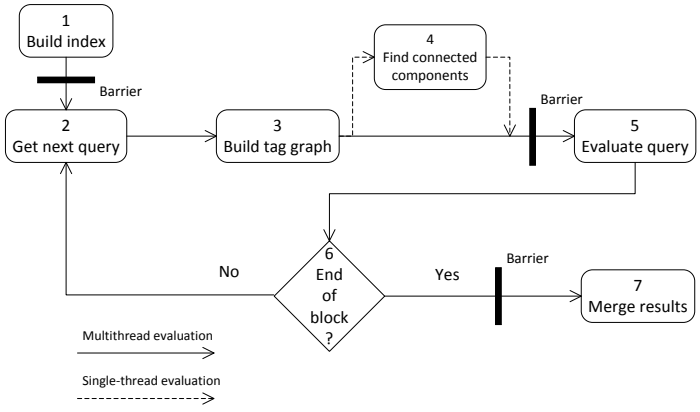

Figure 4: Query type 4 evaluation scheme

Algorithm 11: GBFS

```
1  function gBFS(source, p, h)
       input: source — start vertex,
              p — place to search in,
              h — hops
       output: reached persons from p
       /* Initialization                                              */
2      Q ⟵ source.id ;                                    // Queue
3      hops ⟵ array of -1 that size is size ;             // distances from source
4      rp ⟵ ∅ ;                                           // reached persons
5      Enqueue(Q, source);
6      hops[source.id] ⟵ 0;
7      while Q ≠ ∅ do
8          person ⟵ Dequeue(Q);
9          if hops[person.id] == h then
10             continue;
11         foreach friend of person do
12             if hops[friend.id] == −1 then
13                 Enqueue(Q, friend);
                   // set distance from source
                   hops[friend.id] ⟵ hops[person.id] + 1;
14                 if located_in(friend, p) then
15                     rp ⟵ friend.id;
```

12 Appendix: Tables

Symbol	Definition
$Persons$	set of all people
$Dates$	set of all birthdays of people
G_t	$[l \dots h]$, where $l = \min Dates,\ h = \max Dates$
N_f	the average number of friends of person

Table 1: Summary of notation

1k		10k	
year	count	year	count
1980	82	1980	896
1981	102	1981	991
1982	103	1982	1009
1983	92	1983	979
1984	115	1984	994
1985	117	1985	1000
1986	113	1986	1012
1987	92	1987	1045
1988	83	1988	967
1989	93	1989	1024
1990	8	1990	83

Table 2: Distibution of people by year of birth

	1k		10k		
File name	Size, KB	Lines count	Size, KB	Lines count	Growth rate
comment_hasCreator_person	7 225	632 043	281 303	20 096 289	32
comment_replyOf_comment	6 233	407 921	239 184	12 962 819	32
forum_hasMember_person	8 459	275 909	251 887	7 646 634	28
forum_hasTag_tag	161	14 940	4 753	389 472	26
person	74	1 001	756	10 001	10
person_hasInterest_tag	30	3 560	334	35 294	10
person_isLocatedIn_place	8	1 001	92	10 001	10
person_knows_person	226	29 791	2 827	296 131	10
person_studyAt_organisation	10	793	117	7 996	10
person_workAt_organisation	29	2 188	322	22 215	10
place	60	1 074	191	3 380	3
place_isPartOf_place	8	1 068	26	3 374	3
tag	91	1 458	298	4 567	3
organisation_isLocatedIn_place	10	1 254	27	2 931	2

Table 3: Files statistics